

## Notice for the PhD Viva-Voce Examination

Ms Annie Alex, Registration Number: 2071514, PhD Scholar at the Department of Mathematics, School of Sciences, CHRIST (Deemed to be University) will defend her PhD thesis at the public viva-voce examination on Monday, 10 November 2025 at 11:00 am in Room No. 628, 6<sup>th</sup> Floor, R&D Block, CHRIST (Deemed to be University), Bengaluru – 560029, Karnataka, India.

Title of the Thesis : Study on Secure Equitable Domination in

Graphs

Discipline : Mathematics

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The members of the Research Advisory Committee of the Scholar, the faculty members of the Department and the School, interested experts and research scholars of all the branches of research are cordially invited to attend this open viva-voce examination.

Place: Bengaluru

Date: 03 November 2025

Registrar (Academics)

## **ABSTRACT**

Let v be a node of the graph G that is not in D, where D is a subset of V(G). If every node  $v \in G$  has at least one neighbour in D, then the set D is known as the dominating set (DS) of G. Every other node outside of D is protected by the nodes in D, which isregarded as a set of guards. Suppose D is a DS that holds the properties of both a secure dominating set (SDS) and an equitable dominating set (EDS). In that case, D is considered the secure equitable dominating set (SEDS). Let z be any node of S, where S is a set of dominating nodes of a graph G. If there exists a node w such that  $w \in S$ , (S -z) U  $\{w\}$  is also a dominating set and  $|deg(w) - deg(z)| \le 1$ , then set S is a SEDS. The secure equitable domination number (SEDN) of any graph G is the fewest count of nodes that are required to set up a secure equitable dominating set of G. We studied the SEDN of certain basic classes of graphs and obtained a few refined bounds of the SEDN of this parameter. We also include SEDN bounds based on degree, girth, and diameter. Further, we acquired the bounds of SEDN of the graph operations: the join and the corona. We investigated the limits of SEDN for both the Cartesian and the Kronecker product of graphs.

We began our investigation on the se-subdivision number of a graph. We established the se-subdivision number and the se-multi subdivision number of certain specific classes of graphs.

Additionally, we introduced the concepts of se-subdivision stable graphs and se-subdivision critical graphs. The ideas of the secure domination integrity (SDI) and the secure equitable domination integrity (SEDI) in a graph were explained. Several applications of the concept of secure equitable domination in graphs were discussed. Furthermore, we established the bounds of the parameter for certain chemical structures.

**Keywords:** Secure domination number, Equitable domination number, Secure equitable domination number, Secure equitable subdivision number, Secure Domi- nation Integrity, Secure Equitable Domination Integrity, Join of graphs, Corona of graphs, Silicate structures, Benzoid networks.

## **Publications:**

- 1. A. Annie, V. Sangeetha, Secure equitable subdivision number of graphs, Gulf Journal of Mathematics. DOI: https://doi.org/10.56947/gjom.v17i2.2049
- 2. A. Annie, V. Sangeetha, Secure Equitable Domination in Cartesian Product of Graphs, Discrete Mathematics, Algorithms and Applications. DOI: https://doi.org/10.1142/S1793830925501289
- 3. A. Annie, V. Sangeetha, On the Secure Equitable Domination in Graphs, TWMS J. App. Eng. Math. DOI: https://jaem.isikun.edu.tr/web/images/articles/vol.15.no.9/01.pdf
- 4. A. Annie, V. Sangeetha, Secure Equitability in Chemical Networks, Book title: Graph Theory for Computer Science